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No iteration transitions for pseudomonads

We report on the progress towards a no iteration codification of distributive laws for pseudomonads. This time we present the no iteration codification for a transition from a pseudomonad \mathbb{U} on a 2-category \mathcal{A} to a pseudomonad \mathbb{D} on a 2-category \mathcal{X} along a 2-functor $F: \mathcal{A} \rightarrow \mathcal{X}$. It is well known that such structures correspond to liftings of F to the corresponding algebras of \mathbb{U} and \mathbb{D} . In the known codification for these transitions, one of the coherence conditions necessary is:

$$\begin{array}{ccc}
 D^3 F & \xrightarrow{D^2 r} & D^2 F U \\
 \downarrow mDF & \searrow & \downarrow DrU \\
 D^2 F & \xrightarrow{DmF} & D^2 F \\
 \downarrow mF & \searrow \mu_{\mathbb{D}F} & \downarrow mF \\
 DF & \xrightarrow{r} & FU \\
 & & \downarrow rU \\
 & & DFU^2 \\
 & & \downarrow DFn \\
 & & FU^2 \\
 & & \downarrow Fn \\
 & & FU
 \end{array}
 =
 \begin{array}{ccc}
 D^3 F & \xrightarrow{D^2 r} & D^2 F U \\
 \downarrow mDF & \searrow & \downarrow DrU \\
 D^2 F & \xrightarrow{DmF} & D^2 F \\
 \downarrow mF & \searrow \mu_{\mathbb{D}F} & \downarrow mF \\
 DF & \xrightarrow{r} & FU \\
 & & \downarrow rU \\
 & & DFU^2 \\
 & & \downarrow DFn \\
 & & FU^2 \\
 & & \downarrow Fn \\
 & & FU
 \end{array}$$

and is thus difficult to verify in particular cases. The no iteration codification avoids the iterations of D and U shown in the above picture, and thus it is much easier to handle in particular examples. This is joint work with Adrián Vázquez-Márquez.