

Using adaptor grammars  
to identify synergies  
in the unsupervised acquisition  
of linguistic structure

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June, 2008

# Summary

- *Adaptor grammars* are an extension of PCFGs
  - ▶ set of possible trees defined just as in a PCFG
  - ▶ but learns probabilities of entire subtrees (not just rules)
  - ▶ designed to generalize Goldwater's word segmentation and morphology models
- Subtrees (and their probabilities) learnt depend upon previously generated sentences  $\Rightarrow$  grammar “adapts” to data
- Used to learn words in *unsupervised word segmentation*  
Example:  $y_{\Delta} u_{\Delta} w_{\Delta} a_{\Delta} n_{\Delta} t_{\Delta} t_{\Delta} u_{\Delta} s_{\Delta} i_{\Delta} D_{\Delta} 6_{\Delta} b_{\Delta} U_{\Delta} k$
- By changing base grammar, we can simultaneously learn:
  - ▶ collocations
  - ▶ stem-suffix morphology
  - ▶ syllable structure
- Simultaneously learning collocations and syllable structure *significantly improves word segmentation accuracy*

# Language acquisition as Bayesian inference

$$\underbrace{P(\text{Grammar} \mid \text{Data})}_{\text{Posterior}} \propto \underbrace{P(\text{Data} \mid \text{Grammar})}_{\text{Likelihood}} \underbrace{P(\text{Grammar})}_{\text{Prior}}$$

- Likelihood measures how well grammar describes data
- Prior expresses knowledge of grammar before data is seen
  - ▶ can be very specific (e.g., Universal Grammar)
  - ▶ can be very general (e.g., prefer shorter grammars)
- Posterior is a *distribution* over grammars
  - ▶ expresses uncertainty about which grammar is correct

# Using Bayesian posterior for parsing

- Usually *infinitely many* grammars  $G$  with non-zero probability in posterior  $P(G | D)$  given data  $D$ 
  - ▶ pick one grammar somehow (e.g., MAP), or
  - ▶ *use full posterior distribution for parsing*
- “Integrate out” grammar  $G$  to obtain posterior distribution over parse trees  $T$  given data  $D$

$$P(T | D) = \int P(T | D, G) P(G | D) dG$$

- ⇒ Grammatical inference need not produce an explicit grammar
- We use *Markov Chain Monte Carlo* to sample directly from  $P(T | D)$

# Informal description of Adaptor Grammars

- An Adaptor Grammar is a PCFG where a subset of nonterminals are specified as *adapted*
  - Each adapted nonterminal  $A$  has a user-specified concentration parameter  $\alpha_A$ 
    - ▶ SIGMORPH workshop paper describes how to learn  $\alpha_A$
  - An *unadapted nonterminal*  $U$  expands just as in a PCFG
    - ▶ to children  $V_1 \dots V_m$  with probability  $\theta_{U \rightarrow V_1 \dots V_m}$
  - An *adapted nonterminal*  $A$  expands:
    - ▶ to a previously generated subtree  $t$  rooted in  $A$  with probability  $\propto$  number of times  $t$  was previously selected
    - ▶ to children  $B_1 \dots B_m$  with probability  $\propto \alpha_A \theta_{U \rightarrow V_1 \dots V_m}$
- ⇒ “Rich get richer” power-law distribution over subtrees
- ⇒ A tree can be more probable than the subtrees it contains

## Word segmentation task

- Brent corpus of 9,790 transcribed child-directed utterances of 33,399 words in Bernstein-Ratner corpus
- Phonemic representation from pronouncing dictionary
- Given utterance boundaries but not word boundaries  
Example: *l U k D \* z 6 b 7 w I T h I z h & t*
- Evaluate f-score of recovered words (Goldwater et al, 2006)
- Used MCMC inference procedure from Johnson et al (2007)
  - ▶ Metropolis-within-Gibbs sampler integrating out grammar
  - ▶ samples parses from PCFG approximation (one rule for each previously generated subtree)
  - ▶ clamped concentration parameters  $\alpha_A$  to 1, 10, 100 or 1,000
  - ▶ uniform Dirichlet prior on rule probabilities  $\theta_{U \rightarrow V_1 \dots V_m}$
  - ▶ results averaged over 8 runs of 10,000 epochs each
  - ▶ software available from <http://cog.brown.edu/~mj>

# Unigram adaptor grammar

- Adaptor grammar (adapted nonterminals highlighted):

Sentence  $\rightarrow$  Words

Words  $\rightarrow$  Word

Words  $\rightarrow$  Word Words

Word  $\rightarrow$  Phonemes

Phonemes  $\rightarrow$  Phoneme

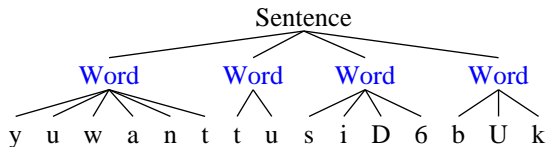
Phonemes  $\rightarrow$  Phoneme Phonemes

*or in abbreviated format:*

Sentence  $\rightarrow$  Word<sup>+</sup>

Word  $\rightarrow$  Phoneme<sup>+</sup>

- Sample parse (only showing root and adapted nonterminals):



- Word segmentation f-score = 0.55 (same as Goldwater et al)
- Can't capture dependencies between words  
 $\Rightarrow$  tends to undersegment

# Unigram word grammar as a Dirichlet Process

- Unigram word grammar implements unigram word segmentation model of Goldwater et al (2006)
- Generative process:
  - ▶ expand Sentence into a sequence of Words using PCFG rules
  - ▶ expand each Word into:
    - a sequence of Phonemes with prob.  $\propto$  number of times Word expanded to this sequence before
    - a sequence of phonemes generated by PCFG rules with prob.  $\propto \alpha_{\text{Word}}$
- This is a *Dirichlet Process* where the PCFG rules expanding Word define the *base distribution*



# Unigram morphology adaptor grammar

- Adaptor grammar memorizes Word, Stem and Suffix:

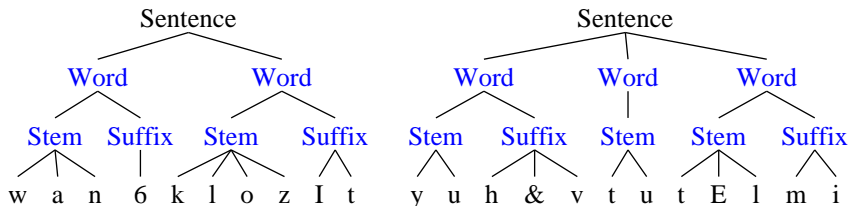
Sentence  $\rightarrow$  Word<sup>+</sup>

Word  $\rightarrow$  Stem (Suffix)

Stem  $\rightarrow$  Phoneme<sup>+</sup>

Suffix  $\rightarrow$  Phoneme<sup>+</sup>

- Sample parse:



- Combines Goldwater's morphology and unigram model
- Word segmentation f-score = 0.46 (worse than unigram)
- Tends to misanalyse words as Stems or Suffixes

# Morphology grammar as a Hierarchical Dirichlet Process

- Expand Sentence into a sequence of Word
- Expand each Word into:
  - ▶ a sequence of Phonemes with prob.  $\propto$  number of times sequence was generated before
  - ▶ a Stem and optional Suffix with prob.  $\propto \alpha_{\text{Word}}$
- Expand Stem into:
  - ▶ a sequence of Phoneme with prob.  $\propto$  number of times Stem expanded to this sequence before
  - ▶ a sequence of Phoneme generated by PCFG rules with prob.  $\propto \alpha_{\text{Stem}}$
- Suffix expands in same way as Stem
- This is a *Hierarchical Dirichlet Process* where Stem and Suffix distributions define the base distribution for Word DP

# Unigram syllable adaptor grammar

- Adaptor grammar distinguishes initial and final syllables

Sentence  $\rightarrow$  Word<sup>+</sup>

Word  $\rightarrow$  SyllableI SyllableF

Syllable  $\rightarrow$  (Onset) Rhyme

SyllableF  $\rightarrow$  (Onset) RhymeF

Rhyme  $\rightarrow$  Nucleus (Coda)

Onset  $\rightarrow$  Consonant<sup>+</sup>

Coda  $\rightarrow$  Consonant<sup>+</sup>

Nucleus  $\rightarrow$  Vowel<sup>+</sup>

Word  $\rightarrow$  SyllableIF

Word  $\rightarrow$  SyllableI Syllable SyllableF

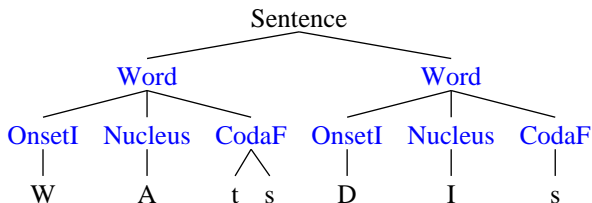
SyllableI  $\rightarrow$  (OnsetI) Rhyme

SyllableIF  $\rightarrow$  (OnsetI) RhymeF

RhymeF  $\rightarrow$  Nucleus (CodaF)

OnsetI  $\rightarrow$  Consonant<sup>+</sup>

CodaF  $\rightarrow$  Consonant<sup>+</sup>



- Word segmentation f-score = 0.52 (also worse than Unigram)

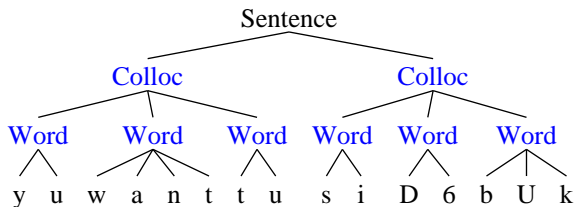
# Collocation adaptor grammar

- Adaptor grammar memorizes collocations (sequences of words) as well as words

Sentence  $\rightarrow$  Colloc<sup>+</sup>

Colloc  $\rightarrow$  Word<sup>+</sup>

Word  $\rightarrow$  Phoneme<sup>+</sup>



- Word segmentation f-score = 0.76 (approx same as Goldwater's bigram model)

# Collocation + morphology adaptor grammar

- Adaptor grammar memorizes collocations, words, stems and suffixes

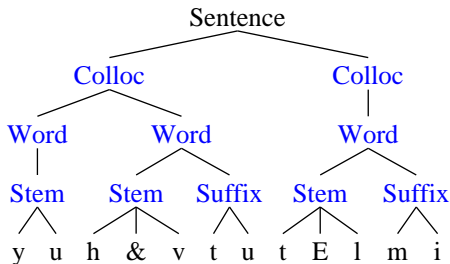
Sentence  $\rightarrow$  Colloc<sup>+</sup>

Colloc  $\rightarrow$  Word<sup>+</sup>

Word  $\rightarrow$  Stem (Suffix)

Stem  $\rightarrow$  Phoneme<sup>+</sup>

Suffix  $\rightarrow$  Phoneme<sup>+</sup>

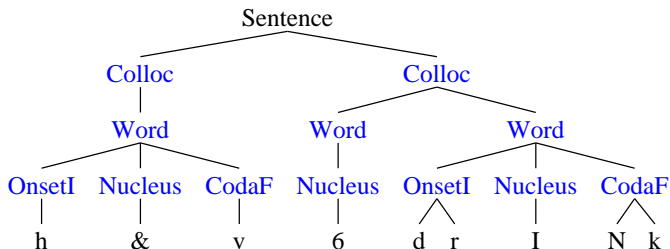


- Word segmentation f-score = 0.73 (worse than Collocation)

# Collocation + syllable adaptor grammar

- Adaptor grammar is combination of collocation and syllable grammars

Sentence  $\rightarrow$  Colloc<sup>+</sup>    Colloc  $\rightarrow$  Word<sup>+</sup>  
Word  $\rightarrow$  (as in syllable grammar)



- Word segmentation f-score = 0.78
- Significantly better ( $p = 0.006$ ) than Collocation on its own

## Word segmentation f-score summary

		Concentration parameter $\alpha$			
		1	10	100	1000
unigram	word	<b>0.55</b>	<b>0.55</b>	<b>0.55</b>	0.53
unigram	morph	<b>0.46</b>	<b>0.46</b>	0.42	0.36
unigram	syll	<b>0.52</b>	0.51	0.49	0.46
collocation	word	0.53	0.64	0.74	<b>0.76</b>
collocation	morph	0.56	0.63	<b>0.73</b>	0.63
collocation	syll	0.77	0.77	<b>0.78</b>	0.74

- Concentration parameter  $\alpha$  tied for all adapted non-terminals

## Conclusion and future work

- Adaptor grammars are a flexible framework for expressing non-parametric Bayesian models
- Probability of a parse depends on how often its subtrees were generated before  $\Rightarrow$  grammar *adapts* to corpus as it parses
- This paper used Adaptor Grammars to develop several models of unsupervised word segmentation
- Confirmed Goldwater's result about importance of modeling intra-word dependencies
- No improvement found in modeling morphology
- Learning collocations and syllable structure in conjunction with word segmentation significantly improves f-score  $\Rightarrow$  synergies in language learning
- In this work concentration parameters  $\alpha$  are fixed, but in further work they are learned  $\Rightarrow$  improves f-score to 0.84



## PCFGs as recursive mixtures

- A PCFG defines distributions  $G_A$  over trees for each  $A \in N \cup T$ 
  - ▶ if  $w \in T$  then  $G_w = \delta_w$  (puts all mass on singleton tree  $w$ )
  - ▶ if  $A \in N$  then

$$G_A = \sum_{A \rightarrow B_1 \dots B_n \in R_A} \theta_{A \rightarrow B_1 \dots B_n} \text{TD}_A(G_{B_1}, \dots, G_{B_n})$$

where  $\text{TD}_A(G_{B_1}, \dots, G_{B_n})$  is the distribution over trees with root label  $A$  satisfying:

$$\text{TD}_A(G_1, \dots, G_n) \left( \begin{array}{c} A \\ \diagdown \quad \diagup \\ t_1 \quad \dots \quad t_n \end{array} \right) = \prod_{i=1}^n G_i(t_i).$$

$\text{TD}_A(G_1, \dots, G_n)$  is the distribution over trees with root node  $A$  and each subtree  $t_i$  is generated *independently* from  $G_i$ .

# Adaptor grammars

- An adaptor grammar is just like a PCFG, except that each adapted nonterminal's distribution is passed through a Dirichlet Process

$$H_A = \sum_{A \rightarrow B_1 \dots B_n \in R_A} \theta_{A \rightarrow B_1 \dots B_n} \text{TD}_A(G_{B_1}, \dots, G_{B_n})$$
$$G_A \sim \text{DP}(\alpha_A, H_A) \quad \text{if } A \text{ is adapted}$$
$$G_A = H_A \quad \text{if } A \text{ is not adapted}$$

- The Dirichlet Process concentrates mass on frequently used subtrees
- Implemented using Chinese Restaurant Processes